



PUBLIC SCHOOL DARBHANGA
SESSION (2020-21)
CLASS-IX
MATHEMATICS
POLYNOMIALS
REVISION

1. Find the value of the polynomial $(x)=5x-4x^2+3$

- (i) $x=0$
- (ii) $x = -1$
- (iii) $x = 2$

2. Find $p(0)$, $p(1)$ and $p(2)$ for each of the following polynomials:

- (i) $p(y)=y^2-y+1$
- (ii) $p(t)=2+t+2t^2-t$
- (iii) $p(x)=x^3$
- (iv) $p(x)=(x-1)(x+1)$

3. Following are zeroes of the polynomial, indicated against them.

- (i) $p(x)=3x+1$, $x=-1$
- (ii) $p(x)=5x-\pi$, $x=\frac{4}{5}$
- (iii) $p(x)=x^2-1$, $x=1, -1$
- (iv) $p(x)=(x+1)(x-2)$, $x= -1, 2$
- (v) $p(x)=x^2$, $x=0$

4. Find the zero of the polynomial in each of the following cases:

- (i) $p(x) = x + 5$
- (ii) $p(x) = x - 5$
- (iii) $p(x) = 2x + 5$
- (iv) $p(x) = 3x - 2$
- (v) $p(x) = 3x$
- (vi) $p(x) = ax$, $a \neq 0$
- (vii) $p(x) = cx + d$, $c \neq 0$, c, d are real numbers.

5. Find the remainder when x^3+3x^2+3x+1 is divided by

- (i) $x+1$
- (ii) $x+\pi$
- (iii) 5

+2x

ANSWER KEY

1. Find the value of the polynomial $(x)=5x-4x^2+3$

- (i) $x=0$
- (ii) $x=-1$
- (iii) $x=2$

Solution:

$$\text{Let } f(x)=5x-4x^2+3$$

(i) When $x=0$

$$\begin{aligned}f(0) &= 5(0)-4(0)^2+3 \\&= 3\end{aligned}$$

(ii) When $x=-1$

$$\begin{aligned}f(x) &= 5x-4x^2+3 \\f(-1) &= 5(-1)-4(-1)^2+3 \\&= -5-4+3 \\&= -6\end{aligned}$$

(iii) When $x=2$

$$\begin{aligned}f(x) &= 5x-4x^2+3 \\f(2) &= 5(2) \\&\quad -4(2)^2+3 \\&= 10-16+3 \\&= -3\end{aligned}$$

2. Find $p(0)$, $p(1)$ and $p(2)$ for each of the following polynomials:

(i) $p(y)=y^2-y+1$

Solution:

$$\begin{aligned}p(y) &= y^2-y+1 \\ \therefore p(0) &= (0)^2-(0)+1=1 \\ p(1) &= (1)^2-(1)+1=1 \\ p(2) &= (2)^2-(2)+1=3\end{aligned}$$

(ii) $p(t)=2+t+2t^2-t^3$

Solution:

$$\begin{aligned}p(t) &= 2+t+2t^2-t^3 \\ \therefore p(0) &= 2+0+2(0)^2-(0)^3=2 \\ p(1) &= 2+1+2(1)^2-(1)^3=2+1+2-1=4 \\ p(2) &= 2+2+2(2)^2-(2)^3=2+2+8-8=4\end{aligned}$$

(iii) $p(x)=x^3$

Solution:

$$\begin{aligned} p(x) &= x^3 \\ \therefore p(0) &= (0)^3 = 0 \\ p(1) &= (1)^3 = 1 \\ p(2) &= (2)^3 = 8 \end{aligned}$$

(iv) $p(x) = (x-1)(x+1)$

Solution:

$$\begin{aligned} p(x) &= (x-1)(x+1) \\ \therefore p(0) &= (0-1)(0+1) = (-1)(1) = -1 \\ p(1) &= (1-1)(1+1) = 0(2) = 0 \\ p(2) &= (2-1)(2+1) = 1(3) = 3 \end{aligned}$$

3. Verify whether the following are zeroes of the polynomial, indicated

against them. (i) $p(x) = 3x+1$, $x = -\frac{1}{3}$

Solution:

$$\text{For, } x = -\frac{1}{3}, p(x) = 3x+1 = -1+1 =$$

$$\begin{aligned} \therefore p\left(-\frac{1}{3}\right) &= 3\left(-\frac{1}{3}\right) + 1 = -1 + 1 = 0 \\ \therefore -\frac{1}{3} &\text{ is a zero of } p(x) \end{aligned}$$

(ii) $p(x) = 5x - \pi$, $x = \frac{4}{5}$

Solution:

$$\text{For, } x = \frac{4}{5}, p(x) = 5x - \pi$$

$$\begin{aligned} \therefore p\left(\frac{4}{5}\right) &= 5\left(\frac{4}{5}\right) - \pi \\ \therefore \frac{4}{5} &\text{ is not a zero of } p(x) \end{aligned}$$

(iii) $p(x) = x^2 - 1$, $x = 1, -1$

Solution:

$$\text{For, } x = 1, -1;$$

$$p(x) = x^2 - 1$$

$$\therefore p(1) = 1^2 - 1 = 1 - 1 =$$

$$0$$

=

$$(-1)^2 - 1 = 1 - 1 = 0$$

$\therefore 1, -1$ are zeros of $p(x)$.

(iv) $p(x) = (x+1)(x-2)$, $x = -1, 2$

Solution:

$$\text{For, } x = -1, 2;$$

$$\begin{aligned}
 p(x) &= (x+1)(x-2) \\
 \therefore p(-1) &= (-1+1)(-1-2) \\
 &= ((0)(-3)) = 0 \\
 p(2) &= (2+1)(2-2) = (3)(0) = 0 \\
 \therefore -1, 2 &\text{ are zeros of } p(x).
 \end{aligned}$$

(v) $p(x) = x^2, x=0$

Solution:

$$\begin{aligned}
 \text{For, } x=0 \quad p(x) &= \\
 x^2 \quad p(0) &= 0^2 = 0 \\
 \therefore 0 &\text{ is a zero of } p(x).
 \end{aligned}$$

4. Find the zero of the polynomial in each of the following cases:

(iii) $p(x) = x + 5$

Solution:

$$\begin{aligned}
 p(x) &= x+5 \\
 \Rightarrow x+5 &= 0 \\
 \Rightarrow x &= -5 \\
 \therefore -5 &\text{ is a zero polynomial of the polynomial } p(x).
 \end{aligned}$$

(iv) $p(x) = x - 5$

Solution:

$$\begin{aligned}
 p(x) &= x-5 \\
 \Rightarrow x-5 &= 0 \\
 \Rightarrow x &= 5 \\
 \therefore 5 &\text{ is a zero polynomial of the polynomial } p(x).
 \end{aligned}$$

(iii) $p(x) = 2x + 5$

Solution:

$$\begin{aligned}
 p(x) &= 2x+5 \\
 \Rightarrow 2x+5 &= 0 \\
 \Rightarrow 2x &= -5 \\
 \Rightarrow x &= -\frac{5}{2}
 \end{aligned}$$

$\therefore x = -\frac{5}{2}$ is a zero polynomial of the polynomial $p(x)$.

(iv) $p(x) = 3x - 2$

Solution:

$$\begin{aligned}
 p(x) &= 3x-2 \\
 \Rightarrow 3x-2 &= 0 \\
 \Rightarrow 3x &= 2
 \end{aligned}$$

$$\Rightarrow x = \frac{2}{3}$$

$\therefore x = \frac{2}{3}$ is a zero polynomial of the polynomial $p(x)$

(v) $p(x) = 3x$

Solution:

$$p(x) = 3x$$

$$\Rightarrow 3x = 0$$

$$\Rightarrow x = 0$$

$\therefore 0$ is a zero polynomial of the polynomial $p(x)$.

(vi) $p(x) = ax, a \neq 0$

Solution:

$$p(x) = ax$$

$$\Rightarrow ax = 0$$

$$\Rightarrow x = 0$$

$\therefore x = 0$ is a zero polynomial of the polynomial $p(x)$.

(vii) $p(x) = cx + d, c \neq 0, c, d$ are real numbers.

Solution:

$$p(x) = cx + d$$

$$\Rightarrow cx + d = 0$$

$$\Rightarrow x = \frac{-d}{c}$$

$\therefore x = \frac{-d}{c}$ is a zero polynomial of the polynomial
 $p(x)$.

5. Find the remainder when $x^3 + 3x^2 + 3x + 1$ is divided by

(iii) $x+1$

Solu

tion:

$$x+1$$

$$= 0$$

$$\Rightarrow x = -1$$

\therefore Remainder:

$$\begin{aligned} p(-1) &= (-1)^3 + 3(-1)^2 + 3(-1) + 1 \\ &= -1 + 3 - 3 + 1 \\ &= 0 \end{aligned}$$

(iv) x

+

π

Solu

tion:

$$x + \pi$$

$$= 0$$

$$\Rightarrow x =$$

$$-\pi$$

∴ Remainder:

$$\begin{aligned} p(0) &= (-\pi)^3 + 3(-\pi)^2 + 3(-\pi) + 1 \\ &= -\pi^3 + 3\pi^2 - 3\pi + 1 \end{aligned}$$

(v) $5+2x$

Solution:

$$5+2x=0$$

$$\Rightarrow 2x=-5$$

$$\Rightarrow x = -\frac{5}{2}$$

